Thermal analysis and optimization of multiple LED packaging based on a general analytical solution

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Multiple-chip packaging becomes common in LEDs packaging community. For such type of packaging, thermal spreading resistance is an important factor to affect the total thermal performance of LEDs. In this study, a general analytical solution is used to study the whole temperature field of LED packaging substrate, this solution is based on the method of variable separation for thermal spreading resistances of eccentric heat sources on a rectangular flux channel. The feasibility of the analytical method used in LEDs packaging has been proven by the temperature comparison with existing experimental and numerical results of an 80 W LED street lamp. By changing the chips arrangement on the substrate, temperature field optimization is conducted with maximal temperature difference of the substrate as the target function. The results show that spreading resistance plays a significant role to affect temperature field. When the LED distributions are effectively designed, the highest temperature on the substrate goes lower and the lowest temperature on the board goes higher, the temperature field becomes uniform, its spreading resistance becomes lower.

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1. Introduction

Light-emitting diodes (LEDs) have many significant advantages, such as high efficiency, good reliability, long lifetime, variable color and low power consumption, therefore, LEDs have begun to play an important role in many applications [1]. Typical applications include back lighting for cell phones and other liquid crystal display (LCD), interior and exterior automotive lighting illumination. In the near future, the biggest area that LED will be used in is general lighting. In energy shortage condition, Chinese authorities estimate that if LEDs dominate the lighting market in 2010, one third of the present lighting power consumption will be saved, which will greatly ameliorate the energy crisis in China [2].

To obtain more lumen, the driving electric current of LED chips grows fastly nowadays. However, as to the high power LED chips, generally nearly 80% of the input power is transformed into heat while the rest is transformed into light. Therefore, during the effort to make LED brighter, lots of heat in LED chips will be generated. Inevitably, the temperature of the LED chips will increase because of this heat. Temperature of LEDs is a primary parameter influencing the reliability and durability [3], high temperature and temperature gradient will generate significant stresses in both materials and along interfaces, if considering the mismatch of Young’s modules and coefficients of thermal expansions (CTEs). Exceeding the maximum rated chip temperature could lead to accelerated light output degradation and sometimes even catastrophic failure. Moreover, LED temperature influences the light output quality. Therefore, to gain a reliable and perfect product with good performance, thermal management of high power LEDs is very important. Temperature of LED chip is a key evaluation parameter of thermal management.

In order to meet the illuminating demand and reduce the cost, LEDs have been packaged in multi-chip packaging modules. Thermal performances of multi-chip modules are different from single chip modules due to the possible non-uniformity in temperature. Research on thermal characteristic of multi-chip LEDs is becoming a new topic. Kim and Shin have introduced the thermal difference of one-chip, two-chip and four-chip designs [4]. The results demonstrate that in multi-chip packaging, the dependence of the thermal resistance and junction temperature on the number of the chips is stronger for the LED package.

For the multi-chip packaging design, spreading thermal resistance should be considered [5,6]. Thermal spreading resistance theory is found to have widespread applications in electronics cooling, both at the board and chip level. These include, but are not
limited to, the prediction of thermal resistance of electronic devices known as ball grid arrays [7], the effect of heat source eccentricity [8], the effect of heat spreaders in compound packages [9–12], the effect of orthotropic properties [13,14], and the issues of contact shape and edge cooling [15–17]. In a multi-chip packaging, huge heat generated from the LED chips is conducted through heat slug to the printed circuit board, and finally is transferred from the heat sink to environment. Thermal spreading resistance of multi-chip packaging which results from discrete heat sources is a key thermal resistance in the above heat transfer process. Yovanovich and Culham’s group has many researches on the spreading resistance of multi-chip packaging, specially in the applications of electronic packaging and reliability. In these studies, Muzychka et al. [8] have proposed a simple method for predicting mean and centroidal heat source temperature. This solution can be used to model any number of discrete heat sources on a compound or an isotropic flux channel. It is finally expressed as

\[ \theta(x, y, z) = T(x, y, z) - T_f \] (1)

where \( T(x, y, z) \) is the layer temperature, and \( T_f \) is the sink temperature. This solution can be used to model any number of discrete heat sources on a compound or an isotropic flux channel. It is finally expressed as

\[
\theta(x, y, z) = A_0 + B_0 z + \sum_{m=1}^{\infty} \cos(\lambda x)A_1 \cosh(\lambda z) + B_1 \sinh(\lambda z) + \sum_{n=1}^{\infty} \cos(\delta y)A_2 \cosh(\delta z) + B_2 \sinh(\delta z) \]

\[
+ \sum_{n=1}^{\infty} \cos(\gamma y)B_3 \cosh(\gamma z) + B_3 \sinh(\gamma z) \]

\[
\times \sum_{n=1}^{\infty} \cos(\alpha x)\cos(\beta y)A_4 \cosh(\alpha z) + B_4 \sinh(\alpha z) \]

(2)

where \( \lambda = \frac{m \pi}{a} \), \( \delta = \frac{n \pi}{b} \), and \( \beta = \sqrt{\delta^2 + \gamma^2} \).

From the above equation, it is found that it contains four components, a uniform flow solution and three spreading solutions which vanish when the heat flux is distributed uniformly over the entire surface \( z = 0 \). Application of the thermal boundary condition at \( z = t_1 \) for an isotropic rectangular plate yields the following result for the Fourier coefficients

\[ B_i = -\phi(\zeta)A_i \quad i = 1, 2, 3 \] (3)

where

\[ \phi(\zeta) = \frac{\zeta \sinh(\zeta t_1) + h/k_1 \cosh(\zeta t_1)}{\zeta \cosh(\zeta t_1) + h/k_1 \sinh(\zeta t_1)} \] (4)

where \( \zeta \) is replaced by \( \lambda, \delta, \beta \). The final coefficients \( A_{m}, A_{n}, A_{mn} \) are obtained by taking Fourier series expansions of boundary condition at the surface \( z = 0 \). This results in the following equations

\[ A_m = \frac{2Q \sin(\frac{\pi}{2a} c_m) - \sin(\frac{\pi}{2a} c_m)}{abcd \cos(\phi(h_n))} \] (5)

\[ A_n = \frac{2Q \sin(\frac{\pi}{2b} d_n) - \sin(\frac{\pi}{2b} d_n)}{abcd \cos(\phi(h_n))} \] (6)

\[ A_{mn} = \frac{16Q \cos(\frac{\pi}{2a} c_m) \sin(\frac{\pi}{2b} d_n) \cos(\phi(h_n)) \sin(\frac{\pi}{2b} d_n)}{abcd \cos(\phi(h_n))} \] (7)

2. Description of analytical solution

Muzychka et al. have presented an analytical general solution based on separation variable method for total thermal spreading resistance of eccentric heat sources on rectangular flux channel [8]. The solution is

\[ \theta(x, y, z) = T(x, y, z) - T_f \] (1)

where \( T(x, y, z) \) is the layer temperature, and \( T_f \) is the sink temperature. This solution can be used to model any number of discrete heat sources on a compound or an isotropic flux channel. It is finally expressed as

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where \( \lambda = \frac{m \pi}{a} \), \( \delta = \frac{n \pi}{b} \), and \( \beta = \sqrt{\delta^2 + \gamma^2} \).

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\[ A_m = \frac{2Q \sin(\frac{\pi}{2a} c_m) - \sin(\frac{\pi}{2a} c_m)}{abcd \cos(\phi(h_n))} \] (5)

\[ A_n = \frac{2Q \sin(\frac{\pi}{2b} d_n) - \sin(\frac{\pi}{2b} d_n)}{abcd \cos(\phi(h_n))} \] (6)

\[ A_{mn} = \frac{16Q \cos(\frac{\pi}{2a} c_m) \sin(\frac{\pi}{2b} d_n) \cos(\phi(h_n)) \sin(\frac{\pi}{2b} d_n)}{abcd \cos(\phi(h_n))} \] (7)

Fig. 1. Schematic diagram of the 80 W LED street lamp.
Finally, values for the coefficients in the uniform flow solution are given by

\[
A_0 = \frac{Q}{\nu \left( \frac{1}{k_1^2} + \frac{1}{h} \right)} \quad (8)
\]

\[
B_0 = \frac{Q}{k_1 \nu} \quad (9)
\]

For multiple heat sources, the solution for the temperature distribution on the surface of the board or heat sink is obtained using superposition. Therefore, there is

\[
\theta_i(x, y, 0) = A_0^i + \sum_{m=1}^{\infty} A_{im}^i \cos(\lambda x) + \sum_{n=1}^{\infty} A_{in}^i \cos(\delta y) + \sum_{m=1}^{\infty} A_{im}^i \cos(\lambda x) \cos(\delta y)
\]

(10)

where \(\theta_i\) is the temperature excess for each heat source by itself. By adding each \(\theta_i\), it is easy to obtain the temperature of each heat sources and the temperature distribution on board or heat sink.

3. Temperature calculation of an 80W LED street lamp

Experiment and numerical simulation of an 80W LED street lamp shown in Fig. 1 have been conducted in the authors’ previous work [2]. The lamp is mainly composed of three parts: twenty high-power LED modules, a mechanical frame for heat dissipation and supporting LED modules. The lamp frame consists of an aluminum base and aluminum fins. Twenty high-power LED modules are directly bonded to the aluminum base. The modules in the central two rows are 3 W LED packaging, each of which includes three 1 W chips inside. The other two rows consist of 5 W LED modules, each of the 5 W packages includes four chips inside, and they are supplied with 5 W power. In the former experiment study, sixteen thermocouples were used to measure the temperature points at the aluminum base and fins. Based on experimental data, the average heat transfer coefficient of natural convection on the lamp is obtained. A numerical model was also proposed based on the experiment results to show the whole temperature field of the lamp. According to the temperature field of numerical analysis shown in Fig. 2, the temperature changes a wide scale in the whole model. It is obvious that a large temperature difference exists between the chip location and the substrate edge. Therefore, spreading resistance cannot be ignored in this multi-chip packaging lamp.

The heat transfer characteristics inside the street lamp are as follows: firstly, LED chip is the heat source; secondly, LED chips are...
eccentric heat sources on rectangular channel; thirdly, LED packaging is based on electronic packaging method and its thermal management methods are mainly heat conduction and convection. According to the heat transfer analysis and the description of the analytical general solution, the equation in the above section is supposed to be suitable to calculate the thermal spreading resistance of this lamp.

In the solution presented by Muzychka et al., eccentric heat sources are on rectangular flux channel, the whole model is a rectangular plate, but in the lamp shown in Fig. 1, the mechanical frame of the lamp is a complicated structure, which needs model simplification. Its heat sink needs to be simplified into a flat plate. Twenty one LED chips in this model are simplified into twenty-one squares, whose sizes are 1 mm by 1 mm. The convection coefficient of the bottom surface on the simplified plate is replaced by an equivalent value which accounts for both the heat transfer in the fin area and the plate area. The other faces encapsulated in lampshade, are supposed to be adiabatic, because there is little part of heat flux passing through them.

To apply the above equations into the present model, heat sink with many fins should be simplified into a plate in heat transfer area. $c$ and $d$ is the length and width of the heat source respectively, which is 1 mm here. $a$ is the real heat transfer coefficient based on the heat sink area including fin area. According to the experimental data obtained in the previous work [2] and based on $Q = \alpha F VT$, the average heat transfer coefficient of natural convection on the lamp is obtained as follows

$$\alpha = \frac{Q}{FVT} = \frac{70}{1.2^4(42 - 11)} \text{W/m}^2 \cdot \text{K} = 1.9 \text{W/m}^2 \cdot \text{K}$$

where $Q$ is the heat, $F$ is the total heat transfer area of the lamp fins and base, which is about 1.2 m$^2$. $VT$ is the temperature difference between the fin and the environment. In the experiments, the steady average temperature of the fin and base was about 42.1 °C. The environment temperature was about 11 °C. Thus, $VT$ is about 31 K. Then its general convection coefficient is 1.9 W/(m$^2$K). In this case, heat sink is simplified into a flat plate (0.6 m by 0.3 m) with the bottom face area of 2.032 m$^2$. $h_{eff}$ is an equivalent natural convection efficient when the heat sink of the street lamp is regarded as a plate without its fins. The relationship between $\alpha$ and $h_{eff}$ is described as $\alpha x = h_{eff}A_b$. $A$ is the total heat sink area that is exposed to the environment. $A_b$ is the heat sink base area, and it does not include the fin area. Based on the equation, equivalent convection coefficient $h_{eff}$ in this simplified model is 25.344 W/(m$^2$K), which depends on fin base area.

After obtaining the basic parameters, a MATLAB program is built to calculate the above equations (1)–(10) and draw the isothermal chart. Firstly, it calculates the temperature excess $\theta_i$ which is caused by the ith LED chip, then adds all $\theta_i$ and ambient temperature to obtain the temperature of the whole LED street lamp. The material of the lamp structure is aluminum, and its thermal conductivity is 160 W/mK.

As the plate is axis symmetric structure, to save calculation time, temperature field of a quarter of the simplified plate area is shown. The calculation section is shown in Fig. 3. Isothermal chart made by the MATLAB program is shown in Figs. 4 and 5.

It is clear from Figs. 4 and 5 that there are six peaks in the temperature field. They are the hottest areas where the LED chips are located. The temperature data of the six peaks is presented in Table 1.

With the same ambient temperature, experimental temperature tested by thermocouple located near the 5 W chip in row 1 is 42.1 °C, and in numerical analysis the corresponding temperatures are 47.11 °C (5 W chip) and 46.11 °C (3 W chip). There are differences between these hottest temperatures obtained by three methods. Temperature calculated by the analytical general solution is much closer to the data obtained by numerical analysis. These differences can be attributed to the measurement location difference. Experiment data was collected by thermocouples placed around LED chip modules. Thermocouples were located next to the chip module and kept small distance from heat generation points, which is due to the limitation of thermocouple distribution.

<table>
<thead>
<tr>
<th>Table 1</th>
<th>Temperature data of six peaks (°C).</th>
</tr>
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<tbody>
<tr>
<td></td>
<td>Under 3 W chip</td>
</tr>
<tr>
<td>Row 1 chip</td>
<td>No. 1</td>
</tr>
<tr>
<td>Row 2 chip</td>
<td>No. 3</td>
</tr>
<tr>
<td>Row 3 chip</td>
<td>No. 5</td>
</tr>
</tbody>
</table>

<table>
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<tr>
<th>Table 2</th>
<th>Temperature comparison under two chip distribution cases.</th>
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<tbody>
<tr>
<td></td>
<td>Highest temperature (°C)</td>
</tr>
<tr>
<td>One chip distribution case</td>
<td>48.4</td>
</tr>
<tr>
<td>Another chip distribution case</td>
<td>45.6</td>
</tr>
</tbody>
</table>
Therefore, the temperature measured by thermocouples was of the surface on heat sink plate which was near the chip, rather than exact chip location temperature. However, for simulation and analytical results, both the temperature data are of the location where actual LED chip was bonded.

To sum up, a general analytical solution can be used to analyze thermal characteristics of the LEDs in multi-chip packaging. It can provide relatively accurate data. Comparing with the above two methods, the present analysis needs less resource and time, it just need do a few changes to the MATLAB program for each case, therefore it is more useful and adaptable for the engineering design, especially for LED engineers since they are not familiar with the heat transfer.

4. Spreading resistance analysis

According to equation (10), the temperature change has a strong relation with heat source locations. A program was built to calculate the total temperature distribution in the LED heat sink plate. In this program, five hundreds and seventy points on heat sink base are picked out to calculate their temperatures. These points uniformly locate on heat sink base in an array with thirty columns and nineteen rows. The program can easily find the highest and the lowest temperature points. The result shows temperature difference of the hottest point and the coldest point on heat sink base changes greatly when heat sources locations change. Table 2 clearly demonstrates this viewpoint. In Table 2, it is found that for different LEDs distribution, maximal temperature differences among the heat sink base change from 5.5 °C to 12.1 °C. It is obvious that LED chip distribution greatly affects the spreading thermal resistance of the present multi-chip LED street lamp. Figs. 6 and 7 show the temperature field of one chip distribution case, where the maximal temperature difference is 5.5 °C. It is found that chip distribution or the heat sources distribution has an obvious impact on temperature uniformity or the spreading thermal resistance of the heat sink base. This proves that the spreading thermal resistance cannot be neglected in multiple chip packaging like the present 80 W LED street lamp.

5. Temperature field optimization

From the isothermal charts shown in Figs. 6 and 7, it is obvious that there is a temperature difference on the plate. It is nearly 5 °C temperature difference. Besides the LED chip locations, temperatures of the middle and lowest parts of the plate are also high. Therefore, the temperature uniformity of the heat sink for the LED street lamp is not satisfactory. It is known that the temperature gradient is very harmful to LED reliability because of the thermal stress. For multi-chip packaging structures, according to the above discussions, changing the location of LED chips is a good method to obtain better temperature uniformity. In order to realize the optimization process, the maximal temperature difference existing on the heat sink plate is defined as objective function.

To find out the optimized chip distance at X coordinate, a loop is used in the calculation program in which the X coordinates of the chips changes incrementally each time. In this case, the chip locations are changed, which are shown in Table 3. In the result shown in Fig. 8, the highest temperature becomes lower. Temperature of the location under 5 W chips is 45.1 °C, and temperature of the location under 3 W chips is 43.5 °C. The temperature difference between 5 W chips and 3 W chips are 1.6 °C. The highest temperature in the model has decreased sharply. The lowest temperature of the plate increases, which has raised nearly 6 °C. Temperature uniformity has an obvious improvement compared with the case shown in Figs. 3 and 4.

In Fig. 8, it is noted that there are still temperature differences between different rows. Therefore, the chip arrangement needs to be treated with further optimization. Here, to realize the above target, compared with the last case, the new calculation program adds another loop to change both the X and Y coordinates together. Finally, the new chip distribution is shown in Table 4, the corresponding temperature field is shown in Fig. 9. It is found from Fig. 9 that temperatures of the 5 W chip locations are 44.8 °C, and temperatures of 3 W chip locations are 43.5 °C. The temperature difference on the board is just 2.31 °C. Comparing with the temperature difference in the last optimization, the chip arrangement is much better.
6. Conclusions

A general analytical solution is introduced to analyze the spreading thermal resistance and temperature distribution of multi-chip LED packaging in this study. The previous results obtained by the experiment of the 80 W LED street lamp, and its numerical analysis are used to compare with those by this general analytical method. The comparison proves that the analytical solution is effective. Based on the temperature distribution analysis, it is found that the spreading resistance strongly depends on the LED chip distribution. Spreading thermal resistance has an important role in thermal optimization of a multiple LED packaging. In order to achieve uniform temperature distribution, the optimization based on the general analytical solution has been conducted with the maximal temperature difference as an objective function, the results shows that it can conveniently provide the optimized chips distribution.

Acknowledgments

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