



# A modified bidirectional thermal resistance model for junction and phosphor temperature estimation in phosphor-converted light-emitting diodes



Yupu Ma, Run Hu<sup>\*</sup>, Xingjian Yu, Weicheng Shu, Xiaobing Luo<sup>\*</sup>

State Key Laboratory of Coal Combustion, School of Energy and Power Engineering, Huazhong University of Science and Technology, Wuhan 430074, China

## ARTICLE INFO

### Article history:

Received 6 September 2016

Received in revised form 15 October 2016

Accepted 16 October 2016

### Keywords:

Bidirectional thermal resistance model

Junction temperature

Phosphor temperature

Phosphor-converted LEDs

## ABSTRACT

Besides the junction temperature, phosphor temperature is another key parameter to characterize the thermal behavior of phosphor-converted light-emitting diodes (pc-LEDs). However, the measurement of phosphor temperature remains a challenge. In this paper, we proposed a modified bidirectional thermal resistance model for the junction and phosphor temperature estimation. Compared with the conventional thermal resistance model, both the heat generation of the phosphor layer and the heat flow through the phosphor layer were further considered in this model. Three LED packaging structures were fabricated and measured to complete the model. The heat generation of the chip and phosphor layer was measured. With varying driving current from 0.05 A to 0.65 A with an increment of 0.1 A, the maximum deviation of the predicted and measured junction and phosphor temperature is less than 1% and 9.2%, respectively, which proves the feasibility of the proposed model for the junction and phosphor temperature estimation.

© 2016 Elsevier Ltd. All rights reserved.

## 1. Introduction

Light-emitting diodes (LEDs) are widely used in general lighting and flat-panel display applications with their advantages of high luminous efficiency, long lifetime and energy saving [1–3]. In order to realize the white light illumination, a yellow phosphor layer is coated on the blue LED chip to convert the blue light to yellow light, and then the converted yellow light mixes up with the transmitted blue light, and eventually generates white light [4–7]. Such a phosphor layer coated structure is called phosphor-converted LEDs (pc-LEDs). During the color conversion process in the phosphor layer, there exists optical energy loss including the Stokes shift loss, the non-unity quantum efficiency of phosphor particles and self-absorption of yellow light by the phosphors [8]. These optical energy loss is transformed into heat, which makes the phosphor layer another heat source in the pc-LEDs. Generally, the phosphor heat generation is quite small compared to the chip heat generation. Yan et al. revealed that about 8% of the input electrical power is converted into heat by the phosphors [9]. However, such small heat in the phosphor layer can also result in extremely high local temperature due to the low thermal conductivity of the phosphor/silicone composite. High phosphor temperature will

reduce the quantum conversion efficiency of the phosphors and therefore lower the luminous efficiency [10]. Moreover, it induces the material property deterioration, local stress, and even delamination, which results in the degradation of reliability and lifetime of pc-LEDs significantly [11]. Luo et al. observed that the highest temperature of the phosphor particles can reach 315.9 °C, resulting in the phosphor quenching or even the silicone carbonization [12]. Therefore, besides the junction temperature, the phosphor temperature is also an important factor to characterize the thermal performance of white pc-LEDs.

However, the phosphor temperature is difficult to measure because the phosphor particles are dispersed in the silicone matrix and the phosphor diameter usually falls in the range of 13–15 μm. The measurement of phosphor temperature has remained a challenging problem for years. There was no experimental measurement of the phosphor temperature until Kim et al. attempted to directly measure the phosphor temperature by a micro thermocouple [13]. At such circumstance, developing alternative method to predict the phosphor temperature is meaningful and urgent.

Thermal resistance model is demonstrated to be an effective tool to predict junction temperature for LED packaging [14–17]. In the conventional model [14–16], it only takes into account of the heat dissipation path from the junction layer, to the heat slug, substrate, and the ambient. Chen et al. [18] proposed a bidirectional thermal resistance model considering the bidirectional heat

<sup>\*</sup> Corresponding authors.

E-mail addresses: [hurun@hust.edu.cn](mailto:hurun@hust.edu.cn) (R. Hu), [luoxb@hust.edu.cn](mailto:luoxb@hust.edu.cn) (X. Luo).

flow on both sides of the LED packaging structure and improved the accuracy of junction temperature estimation. But they did not consider the heat generation of the phosphor layer in the model. Actually, for pc-LEDs, the heat produced in the phosphor layer cannot be ignored. To solve this problem, Juntunen et al. [19] developed an improved model and considered the heat generation of phosphor layer, but here they think both the heat from the phosphor and the chip transfers from the leadframe to the ambient. Additionally, their model only focused on junction temperature estimation and did not calculate phosphor temperature.

In this work, a modified bidirectional thermal resistance model considering both the heat generation of the phosphor layer and the heat flow through the phosphor layer is proposed to estimate the junction and phosphor temperature for pc-LEDs. Experimental measurements are conducted to validate the model.

## 2. Model establishment

The modified model is established based on the comparison of three LED packaging structures: (I) LED chip without coating, (II) with silicone coating, and (III) with phosphor coating (i.e., pc-LED), respectively, as shown in Fig. 1. Fig. 2 illustrates the schematic of the heat flow path and the corresponding thermal resistance model of these three packaging structures.

For LED chips without any coating, one-dimensional thermal resistance model is applied, as shown in Fig. 2(I). The LED packaging structure is simplified by neglecting the internal structure and only considering a bare chip attached to a substrate with die attach adhesive (DAA). Heat generated in the chip layer is transferred from the junction layer to the ambient through conduction and convection. In this case, the total junction-to-ambient thermal resistance  $R_{1j-a}$  is introduced to define the ratio of the temperature difference between junction temperature  $T_j$  and ambient temperature  $T_a$ , to the total heat flux  $Q_{chip}$ , which can be expressed as:

$$R_{1j-a} = \frac{T_j - T_a}{Q_{chip}} \quad (1)$$

For LED chips with silicone coating, a bidirectional thermal resistance model is applied, as shown in Fig. 2(II). There are two heat transfer paths from the junction to the ambient, namely, the lower path and the upper path. The lower path refers to the conventional pathway which is from junction through substrate to the ambient and the corresponding thermal resistance is  $R_{j-s-a}$ . And the upper path is from the junction layer through silicone coating layer to the ambient and the corresponding thermal resistance is  $R_{sili}$ . In this way, the thermal resistance of the adding silicone layer  $R_{sili}$  is connected with  $R_{j-s-a}$  in parallel. It is noted that  $R_{j-s-a}$  can be regarded as equal to  $R_{1j-a}$  for the same series of LEDs. Knowing the total junction-to-ambient thermal resistance  $R_{1j-a}$  and  $R_{2j-a}$ , we can calculate  $R_{sili}$  as:

$$R_{sili} = \frac{1}{1/R_{2j-a} - 1/R_{1j-a}} \quad (2)$$

For LED chip with phosphor coating, a modified bidirectional thermal resistance model is proposed, as shown in Fig. 2(III). Besides the chip heat generation  $Q_{chip}$ , there is another heat source, namely the phosphor heat generation  $Q_{phos}$ . In order to express the added heat source, it is necessary to introduce the phosphor node  $T_{ph}$  which is defined as the highest temperature in the phosphor layer. We assume that all the heat dissipation of phosphor layer is generated at the phosphor node. Then  $Q_{phos}$  is divided into two parts, namely, one is from the phosphor node to the ambient  $Q_{ph-a}$  through  $R_{ph-a}$ , and the other is from the phosphor node to the junction node  $Q_{ph-j}$  through  $R_{ph-j}$ . And the heat flux component  $Q_{ph-j}$  and  $Q_{chip}$  gather into  $Q_{j-a}$ , then continues conducting downward to the ambient node. Hence, there are three heat flow branches and the heat flux of each branch satisfies the following two equations:

$$Q_{ph-a} + Q_{ph-j} = Q_{phos} \quad (3)$$

$$Q_{ph-j} + Q_{chip} = Q_{j-a} \quad (4)$$

In order to calculate  $T_{ph}$ , we should firstly determine several parameters, including  $T_a$ ,  $Q_{chip}$ ,  $Q_{phos}$ ,  $R_{j-s-a}$ ,  $R_{ph-j}$  and  $R_{ph-a}$ . The ambient temperature  $T_a$  is usually a constant which can be measured easily.  $Q_{chip}$  and  $Q_{phos}$  can be calculated by the output optical power comparison between packaging structure (II) and (III). As for the thermal resistance  $R_{j-s-a}$ ,  $R_{ph-j}$  and  $R_{ph-a}$ , indirect measurements can be applied to acquire these variables. Thermal transient tester (T3ster) is used for thermal characterization of those three packaging structures, of which the total junction-to-ambient thermal resistance is  $R_{1j-a}$ ,  $R_{2j-a}$  and  $R_{3j-a}$ , respectively. We can assume that the thermal resistance from the junction through the substrate to the ambient  $R_{j-s-a}$  of three packaging structures are all approximately equal to  $R_{1j-a}$ , which can be expressed as:

$$R_{1j-s-a} = R_{2j-s-a} = R_{3j-s-a} = R_{1j-a} \quad (5)$$

For packaging structure (II) and (III), the thermal resistance of the added coating can be regarded approximately as equal, as long as two conditions are satisfied, namely, one is that both the coating share the same morphology and the other is that the phosphor volume fraction is not too high so that the thermal conductivity difference between the silicone and phosphor coating is negligible. According to Yuan's work [20,21], thermal conductivity of the phosphor/silicone composite remains stable with a slight rise when phosphor volume fraction is below 40 vol.%. In this case, the following relationships are obtained:

$$R_{ph-j} + R_{ph-a} = R_{sili} \quad (6)$$

The next step is to solve the two variables  $R_{ph-j}$  and  $R_{ph-a}$ . Based on the proposed model, junction temperature  $T_j$  can be calculated as follows:

$$T_j = T_a + R_{1j-a} \cdot Q_{j-a} \quad (7)$$

In addition, the difference between  $T_j$  and  $T_a$  can be calculated by the product of  $R_{3j-a}$  and the total heat generation of the

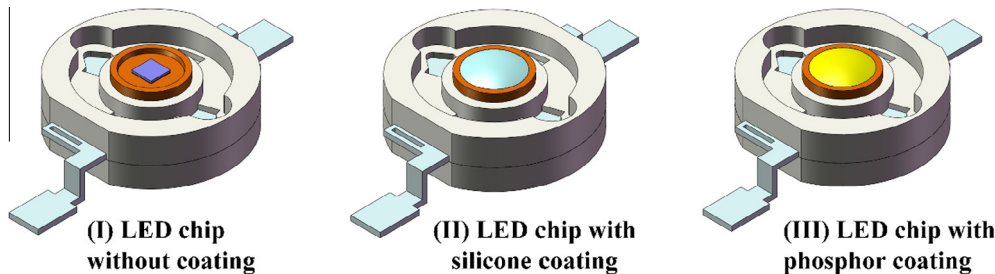


Fig. 1. Schematic of three LED packaging structures (I) LED chip without coating, (II) with silicone coating, and (III) with phosphor coating.

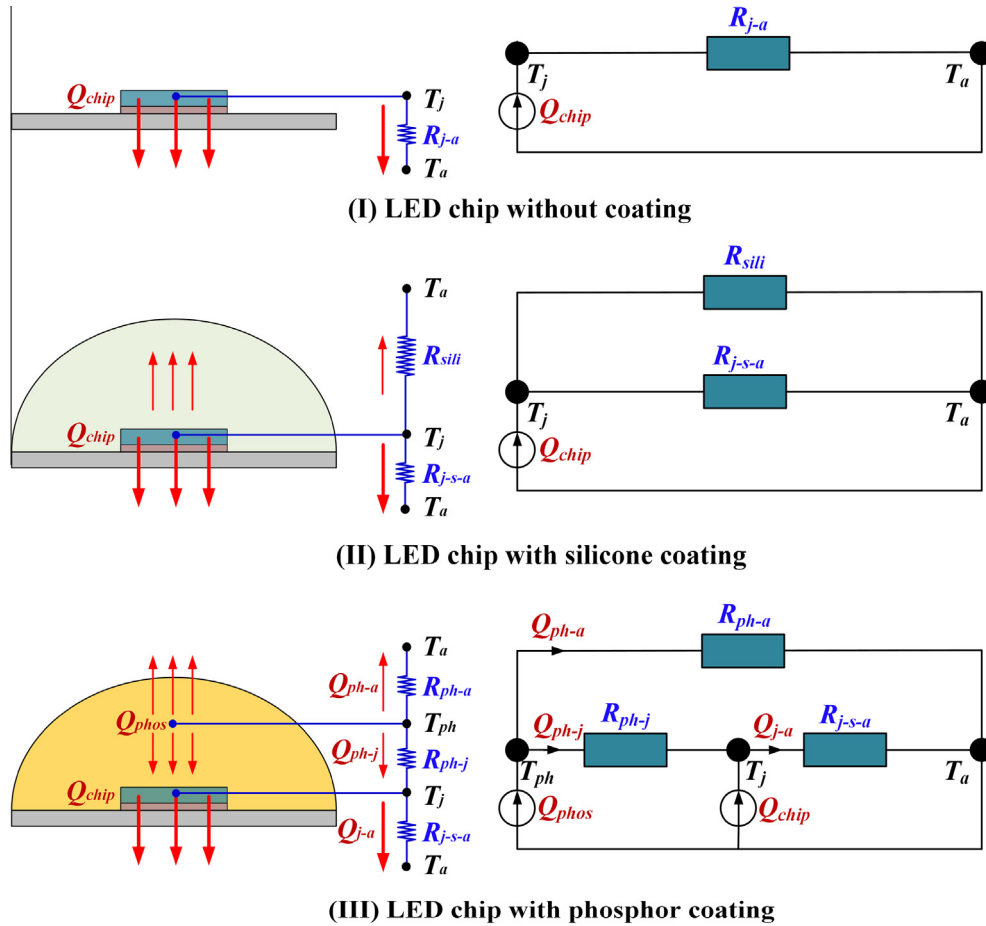


Fig. 2. Schematic of the heat flow path (left) and the corresponding thermal resistance model (right) for three LED packaging structures.

pc-LED, namely the sum of  $Q_{chip}$  and  $Q_{phos}$  [18]. Therefore,  $T_j$  can be acquired as follows:

$$T_j = T_a + R_{3j-a} \cdot (Q_{chip} + Q_{phos}) \quad (8)$$

Combining (7) and (8), we can calculate  $Q_{j-a}$  as follows:

$$Q_{j-a} = \frac{(Q_{chip} + Q_{phos}) \cdot R_{3j-a}}{R_{1j-a}} \quad (9)$$

Substituting (9) to (4), we can acquire  $Q_{ph-j}$  as:

$$Q_{ph-j} = Q_{j-a} - Q_{chip} \quad (10)$$

Substituting (10) to (3), we can also acquire  $Q_{ph-a}$  as:

$$Q_{ph-a} = Q_{ph} - Q_{ph-j} \quad (11)$$

According to the model, the phosphor temperature  $T_{ph}$  can be obtained by either (12) or (13):

$$T_{ph} = T_a + Q_{ph-a} \cdot R_{ph-a} \quad (12)$$

$$T_{ph} = T_j + Q_{ph-j} \cdot R_{ph-j} \quad (13)$$

Combining (6), (8), (12), and (13),  $R_{ph-a}$  and  $R_{ph-j}$  can be calculated as:

$$R_{ph-a} = \frac{R_{3j-a} \cdot (Q_{phos} + Q_{chip}) + R_{sili} \cdot Q_{ph-j}}{Q_{phos}} \quad (14)$$

$$R_{ph-j} = R_{sili} - R_{ph-a} \quad (15)$$

Till then, all the unknown variables are obtained and the junction and phosphor temperature for pc-LED can be calculated via (7) and (12), respectively.

### 3. Experimental validation

To validate the above model, three LED packaging structures were fabricated, as shown in Fig. 1. Each packaging structure possesses five samples. A volume-controlled dip-transfer coating process was applied [22] to ensure that the geometry consistency of the silicone and phosphor layer. Both the silicone and phosphor are directly coated onto the LED chip and the phosphor volume fraction is 8.5 vol.%.

To start with, the optical measurement was conducted by an integrating sphere to calculate  $Q_{chip}$  and  $Q_{phos}$ . The input electrical power  $P_{elec}$  and output optical power  $P_{opt}$  of packaging structures (II) and (III) under varying driving currents were directly measured. For those LED samples from the same batch,  $P_{elec}$  of both packaging structures under a same current is nearly equal. The output optical power of those two structures is donated as  $P_{2,opt}$  and  $P_{3,opt}$ , respectively. Because the silicone and phosphor coating share the same geometry, the output optical power from LED chip and  $Q_{chip}$  of both structures can be regarded as equal. Moreover, when the blue light penetrates the silicone and phosphor layer, optical power loss can be defined as the difference of  $P_{2,opt}$  and  $P_{3,opt}$ . And it is assumed that all the optical loss is occurred in the phosphor layer and converted into heat  $Q_{phos}$ , on the condition that the heat generation in substrate surface is negligible due to its high reflectance and low absorption [23]. So  $Q_{chip}$  and  $Q_{phos}$  can be calculated as follows:

$$Q_{chip} = P_{elec} - P_{2,opt} \quad (16)$$

$$Q_{phos} = P_{2,opt} - P_{3,opt} \quad (17)$$

Secondly, T3ster was used to measure the total junction-to-ambience thermal resistance of three packaging structures. Fig. 3 illustrates the experimental LED apparatus. The LED packages were attached to a designed heat sink by the thermal grease, and the heat sink had a controlled temperature of 30 °C, which was close to the ambient temperature of 29.8 °C. The thermal resistance of LED models can be obtained by evaluating the distribution of RC networks [24]. Before measurement, voltage-temperature-sensitive parameter calibration was conducted. A small current of 1 mA was applied to a temperature-controlled heat sink at different ambient temperature from 25 °C to 75 °C with an increment of 10 °C. And the measured voltage-temperature coefficient was  $-1.3$  mV/K. The heating current for the packaging structure was from 0.05 A to 0.65 A with an interval of 0.1 A and the heating/cooling time was 20 min to ensure that the thermal stabilization was reached. In this way, the junction temperature under different driving currents can be measured.

To further verify the predicted phosphor temperature, an IR camera (FLIR SC620) was used as well. At first, the emissivity of the phosphor layer surface was calibrated and set to be 0.95. Surface temperature distribution under varying current from 0.05 A to 0.65 A with an interval of 0.1 A were obtained in the form of thermal image, in which the maximum temperature was regarded as the phosphor temperature. In this way, phosphor temperature can be measured.

4. Results and discussions

Fig. 4 shows the calculated  $Q_{chip}$  and  $Q_{phos}$  for packaging structure (III) versus driving current based on (16) and (17). It can be seen that  $Q_{chip}$  is always higher than  $Q_{phos}$ . Under the driving current of 0.65 A,  $Q_{chip}$  is about 2.5 times more than  $Q_{phos}$ , which proves that, compared with  $Q_{phos}$ , most of the heat is generated in the chip layer for pc-LEDs. Fig. 5 shows the cumulative structural function curves of three LED packaging structures under the driving current of 0.35 A. It is assumed that  $R_{1j-a}$ ,  $R_{2j-a}$  and  $R_{3j-a}$  are independent on the driving current. The measured results show that the average values of  $R_{1j-a}$ ,  $R_{2j-a}$  and  $R_{3j-a}$  are 12.37 K/W, 12.19 K/W and 11.05 K/W, respectively.

By means of the proposed model, the junction temperature and phosphor temperature can be calculated with the parameters obtained in Figs. 4 and 5. Fig. 6 illustrates the calculated and measured  $T_j$  and  $T_{ph}$  versus driving current. It can be seen that, for direct coted pc-LED, the calculated  $T_{ph}$  is always higher than the calculated  $T_j$ , which agrees with the findings of Yan's work [9]. And the rising rate of  $T_{ph}$  with current is obviously higher than that of  $T_j$ , which implies that phosphor temperature is more sensitive to

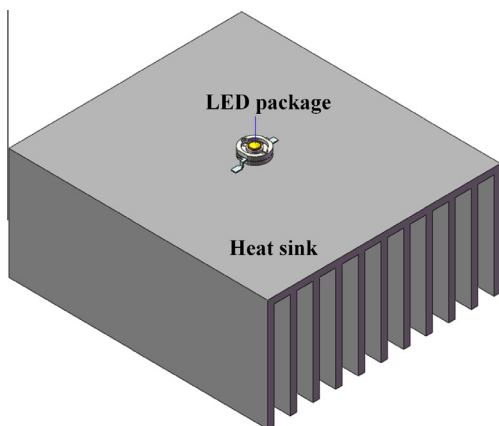


Fig. 3. Schematic of the experimental LED apparatus.

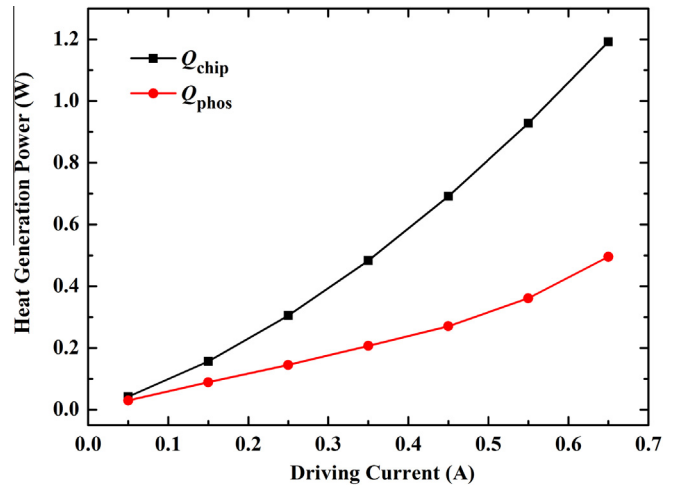


Fig. 4. The calculated  $Q_{chip}$  and  $Q_{phos}$  for packaging structure (III) versus driving current.

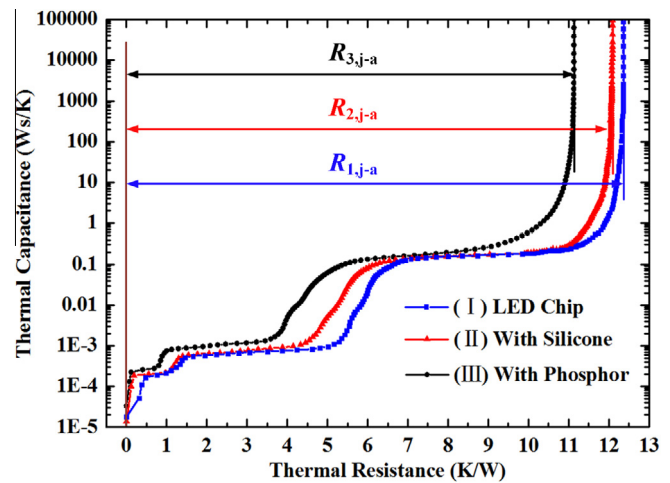


Fig. 5. The cumulative structural function curves of three LED packaging structures.

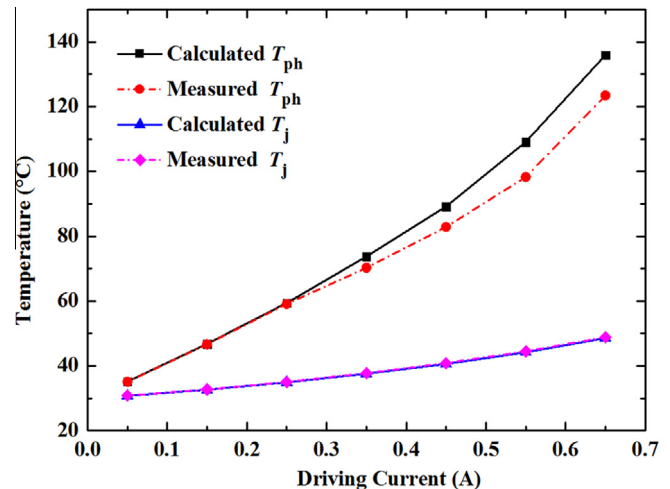


Fig. 6. The calculated and measured  $T_j$  and  $T_{ph}$  versus driving current.

current than junction temperature. It can be explained that  $R_{ph-a}$  is ten or more times than  $R_{j-a}$ , based on (7) and (12), rise of  $Q_{ph-a}$  and  $Q_{j-a}$  caused by increased current will lead to a sharper increase of  $T_{ph}$  than  $T_j$ . Under the driving current of 0.65 A, the calculated  $T_{ph}$



can reach 134.1 °C, which is 85.5 °C higher than the calculated  $T_j$ . When the current keeps rising,  $T_{ph}$  will exceed thermal quenching temperature of phosphors, thus leads to the failure of LED. Hence, phosphor temperature should be paid more attention in LED design and manufacturing process.

From the comparison between the calculated and measured  $T_j$ , it can be found that the maximum deviation between calculated and measured  $T_j$  was less than 1%, which means the calculation agrees pretty well with the measurement.

The measured  $T_{ph}$  obtained by the infrared thermal imager (FLIR SC620) under different currents is shown in Fig. 7. The red cursor is located at the center of the overview of LED package and its temperature is denoted as measured  $T_{ph}$ . As for the comparison between the calculated and measured  $T_{ph}$ , it can be seen that in Fig. 6, when the driving current is below 0.25 A, the temperature difference between calculation and measurement is quite small. However, as the driving current is over 0.25 A, the difference increases with rising current. And the temperature difference can reach 12.5 °C with a corresponding deviation of 9.2% when the current is 0.65 A. It can be explained that IR can only capture the surface temperature distribution of the phosphor layer, but the maximum phosphor temperature is usually located in the internal phosphor layer [9] due to the convective cooling effect on the outer surface. Therefore, the measured  $T_{ph}$  by IR is slightly lower than the calculated  $T_{ph}$ . We admit that it is better to calculate the surface temperature and to compare it with the measured phosphor temperature. But the surface temperature cannot be achieved by the present methods. It is very hard to calculate the field temperatures due to the thin phosphor layer and too many parameters coupling.

It should be noted that the temperature in this model is the maximum value, however the temperatures at different locations in the phosphor layer are different, so this model cannot precisely reflect the effect of the location on the phosphor temperature. There are some factors affecting the accuracy of the model, e.g., the heat generation  $Q_{chip}$  and  $Q_{phos}$ , and the thermal resistances  $R_{1j-a}$ ,  $R_{2j-a}$  and  $R_{3j-a}$ .

In summary, the calculated  $T_j$  and  $T_{ph}$  agreed well with the measured  $T_j$  and  $T_{ph}$ , which proved the efficiency and accuracy of the proposed model for junction and phosphor temperature estimation. With the development of high-brightness pc-LEDs driven by high forward current, local high phosphor temperature will be a key limiting factor of the high reliability and long lifetime of LED luminaries. This modified model contributes to thermal design

and packaging process improvement for reducing phosphor temperature and better thermal & optical performance of pc-LEDs.

## 5. Conclusion

In this work, we proposed a modified bidirectional thermal resistance model for junction and phosphor temperature prediction for pc-LEDs. The model considered the heat transfer path through the phosphor layer to the ambient and the heat generation in phosphor layer simultaneously. It covered an overall concept of heat flow and thermal resistance analysis of pc-LEDs. The junction and phosphor temperature under varying driving current from 0.05 A to 0.65 A and the constant ambient temperature of 30 °C were calculated. The modified model was validated by experiments and the calculation results agree well with the experimental results. The results show that under driving current of 0.65 A, the phosphor temperature reaches 134.1 °C, which is 85.5 °C higher than the junction temperature. We also observed that the increasing rate of phosphor temperature with rising driving current is higher than that of junction temperature, which implies that, for high-power pc-LEDs, better thermal design or packaging process is needed for lower phosphor temperature.

## Acknowledgement

The authors would like to acknowledge the financial support by National Natural Science Foundation of China (51576078, 51606074) and by the Fundamental Research Funds for the Central Universities (2016JCTD112).

## References

- [1] X.B. Luo, R. Hu, S. Liu, K. Wang, Heat and fluid flow in high-power LED packaging and applications, *Prog. Energy Combust.* 56 (2016) 1–32.
- [2] E.F. Schubert, J.K. Kim, H. Luo, J.Q. Xi, Solid state lighting—a benevolent technology, *Rep. Prog. Phys.* 69 (12) (2006) 3069–3099.
- [3] B. Xie, R. Hu, X.B. Luo, Quantum dots-converted light-emitting diodes packaging for lighting and display: status and perspectives, *J. Electron. Packag.* 138 (2) (2016) 020803.
- [4] H. Zheng, X.B. Luo, R. Hu, B. Cao, X. Fu, Y.M. Wang, S. Liu, Conformal phosphor coating using capillary microchannel for controlling color deviation of phosphor-converted white light-emitting diodes, *Opt. Exp.* 20 (5) (2012) 5092–5098.
- [5] X.J. Yu, B. Xie, Q. Chen, Y.P. Ma, R.K. Wu, X.B. Luo, Thermal remote phosphor coating for phosphor-converted white light-emitting diodes, *IEEE Trans. Compon. Packag. Manuf.* 5 (9) (2015) 1253–1257.
- [6] C. Yuan, L. Li, B. Duan, B. Xie, Y.M. Zhu, X.B. Luo, Locally reinforced polymer-based composites for efficient heat dissipation of local heat source, *Int. J. Therm. Sci.* 102 (2016) 202–209.
- [7] R. Hu, X.B. Luo, S. Liu, Study on the optical properties of conformal coating LED by Monte Carlo simulation, *IEEE Photonics Technol. Lett.* 23 (22) (2011) 1673–1675.
- [8] B.J. Shih, S.C. Chiou, Y.H. Hsieh, C.C. Sun, T.H. Yang, S.Y. Chen, T.Y. Chung, Study of temperature distributions in pc-WLEDs with different phosphor packaging structures, *Opt. Exp.* 23 (26) (2015) 33861–33869.
- [9] B. Yan, N.T. Tran, J.P. You, F.G. Shi, Can junction temperature alone characterize thermal performance of white LED emitters?, *IEEE Photonics Technol. Lett.* 23 (9) (2011) 555–557.
- [10] M. Arik, S. Weaver, C. Becker, M. Hsing, A. Srivastava, Effects of localized heat generations due to the color conversion in phosphor particles and layers of high brightness light emitting diodes, *Proc. IEPTCE 35015* (2003) 611–619.
- [11] E.F. Schubert, *Light Emitting Diode*, second ed., Cambridge University Press, New York, 2006 (Chap. 2).
- [12] X.B. Luo, X. Fu, F. Chen, H. Zheng, Phosphor self-heating in phosphor converted light emitting diode packaging, *Int. J. Heat Mass Transfer* 58 (1–2) (2013) 276–281.
- [13] J.H. Kim, M.W. Shin, Thermal behavior of remote phosphor in light-emitting diode packaging structures, *IEEE Electron Dev. Lett.* 36 (8) (2015) 832–834.
- [14] X.B. Luo, Z.M. Mao, J. Yang, S. Liu, Engineering method for predicting junction temperatures of high-power light-emitting diodes, *IET Optoelectron.* 6 (5) (2012) 230–236.
- [15] M. Ha, S. Graham, Development of a thermal resistance model for chip-on-board packaging of high power LED arrays, *Microelectron. Reliab.* 52 (5) (2012) 836–844.

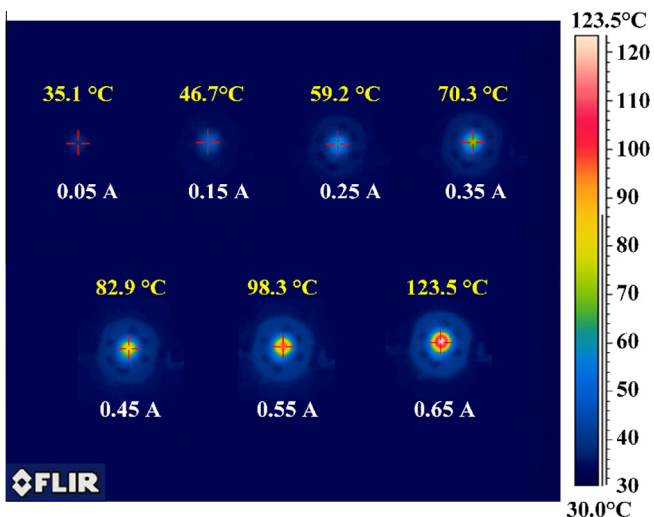


Fig. 7. Measured temperature fields of packaging structure (III) under varying driving currents.

- [16] X. Fu, R. Hu, X.B. Luo, An engineering method to estimate the junction temperatures of light-emitting diodes in multiple LED application, *J. Korean Phys. Soc.* 65 (2) (2014) 176–184.
- [17] H.T. Chen, Y.J. Lu, Y.L. Gao, H.B. Zhang, Z. Chen, The performance of compact thermal models for LED package, *Thermochim. Acta* 488 (1–2) (2009) 33–38.
- [18] H.T. Chen, S.C. Tan, S.Y.R. Hui, Analysis and modeling of high-power phosphor-coated white light-emitting diodes with a large surface area, *IEEE Trans. Power Electron.* 30 (6) (2015) 3334–3344.
- [19] E. Juntunen, O. Tapaninen, A. Sitomaniemi, V. Heikkinen, Effect of phosphor encapsulant on the thermal resistance of a high-power COB LED packaging structure, *IEEE Trans. Compon. Packag. Manuf.* 3 (7) (2013) 1148–1154.
- [20] C. Yuan, X.B. Luo, A unit cell approach to compute thermal conductivity of uncured silicone/phosphor composites, *Int. J. Heat Mass Transfer* 56 (2013) 206–213.
- [21] C. Yuan, B. Xie, M.Y. Huang, R.K. Wu, X.B. Luo, Thermal conductivity enhancement of platelets aligned composites with volume fraction from 10% to 20%, *Int. J. Heat Mass Transfer* 94 (2016) 20–28.
- [22] X.J. Yu, B. Xie, B.F. Shang, Q. Chen, X.B. Luo, A cylindrical tuber encapsulant geometry for enhancing optical performance of chip-on-board packaging light-emitting diodes, *IEEE Photonics J.* 8 (3) (2016) 1600709.
- [23] B. Xie, R. Hu, X.J. Yu, B.F. Shang, Y.P. Ma, X.B. Luo, Effect of packaging method on performance of light-emitting diodes with quantum dot phosphor, *IEEE Photonics Technol. Lett.* 28 (10) (2016) 1115–1118.
- [24] G. Farkas, Q.V. Vader, A. Poppe, G. Bognar, Thermal investigation of high power optical devices by transient testing, *IEEE Trans. Compon. Packag. Manuf.* 28 (1) (2005) 45–50.